$$\frac{1}{3}\log(ax+by)+\log(ax-by)=\frac{1}{2}[\log(\sqrt{ax}+\sqrt{by})+\log(\sqrt{ax}-\sqrt{by})]$$

$$\log\ x-\log\ a=\log\ y-\log\ b$$