

$$\begin{aligned}\frac{1}{3} \log(ax+by)+\log(ax-by) &= \frac{1}{2}[\log(\sqrt{ax}+\sqrt{by})+\log(\sqrt{ax}-\sqrt{by})] \\ \log x-\log a &= \log y-\log b\end{aligned}$$