A unit cube $A B C D E F G H$ (see the figure) is cut by a plane $\mathcal{S}$ that intersects the edges $A B$ and $A D$ at the points $P$ and $Q$ respectively, such that $A P=A Q=x(0<x<1)$. Let the common point of the edge $B F$ and $\mathcal{S}$ be $R$. What is the distance $B R$ if $\angle Q P R=120^{\circ}$ ?


