

$$(1) \quad |\cos B_0 M C_0| = \frac{|MB_0^2 + MC_0^2 + B_0 C_0^2|}{2MB_0 \cdot MC_0} = \frac{1}{2}$$
$$AC_0 = \frac{AC_1}{2} + \frac{AC_2}{2} = \frac{bc}{2(b+a)} + \frac{bc}{2(b-a)} = \frac{b^2c}{b^2-a^2},$$
$$MC_0 = C_1C_0 = \frac{AC_2 - AC_1}{2} = \frac{abc}{b^2 - a^2};$$
$$AB_0 = \frac{c^2 b}{c^2 - a^2}, \quad MB_0 = B_1 B_0 = \frac{abc}{c^2 - a^2}.$$
$$\begin{aligned} & |(MB_0^2 - AB_0^2) + (MC_0^2 - AC_0^2) + 2AB_0 \cdot AC_0 \cos \alpha| = \\ & = \left| -\frac{b^2c^2}{c^2 - a^2} - \frac{b^2c^2}{b^2 - a^2} + \frac{b^2c^2(b^2 + c^2 - a^2)}{(b^2 - a^2)(c^2 - a^2)} \right| = \frac{a^2b^2c^2}{(b^2 - a^2)(c^2 - a^2)} = MB_0 \cdot MC_0, \end{aligned}$$

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