

$$\frac{1}{3} \log(ax + by) + \log(ax - by) = \frac{1}{2} [\log(\sqrt{ax} + \sqrt{by}) + \log(\sqrt{ax} - \sqrt{by})]$$
$$\log x - \log a = \log y - \log b$$