

The angle bisectors drawn from the vertices A and B of a triangle ABC intersect the opposite sides at A_1 and B_1 , respectively. P is the intersection of the ray A_1B_1 with the circumscribed circle of the triangle. Prove that

$$\frac{1}{PA} = \frac{1}{PB} + \frac{1}{PC}.$$